

# Mark Scheme (Results)

Summer 2018

Pearson Edexcel International GCSE In Mathematics B (4MB0) Paper 02

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June 2018
Publications Code 4MB0\_02\_1806\_MS
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# **General Marking Guidance**

- All candidates must receive the same treatment. Examiners must mark the first candidate in exactly the same way as they
  mark the last.
- Mark schemes should be applied positively. Candidates must be rewarded for what they have shown they can do rather than penalised for omissions.
- Examiners should mark according to the mark scheme not according to their perception of where the grade boundaries may lie.
- There is no ceiling on achievement. All marks on the mark scheme should be used appropriately.
- All the marks on the mark scheme are designed to be awarded. Examiners should always award full marks if deserved, i.e. if the answer matches the mark scheme.
  - Examiners should also be prepared to award zero marks if the candidate's response is not worthy of credit according to the mark scheme.
- Where some judgement is required, mark schemes will provide the principles by which marks will be awarded and exemplification may be limited.
- When examiners are in doubt regarding the application of the mark scheme to a candidate's response, the team leader must be consulted.
- Crossed out work should be marked UNLESS the candidate has replaced it with an alternative response.

# Types of mark

o M marks: method marks

A marks: accuracy marks

o B marks: unconditional accuracy marks (independent of M marks)

#### Abbreviations

- o cao correct answer only
- o ft follow through

- o isw ignore subsequent working
- o SC special case
- o oe or equivalent (and appropriate)
- o dep dependent
- o indep independent
- eeoo each error or omission

#### No working

If no working is shown then correct answers normally score full marks

If no working is shown then incorrect (even though nearly correct) answers score
no marks.

### With working

If there is a wrong answer indicated always check the working in the body of the script and award any marks appropriate from the mark scheme.

If it is clear from the working that the "correct" answer has been obtained from incorrect working, award 0 marks.

Any case of suspected misread loses two A (or B) marks on that part, but can gain the M marks. Mark all work on follow through but enter AO (or BO) for the first two A or B marks gained.

If working is crossed out and still legible, then it should be given any appropriate marks, as long as it has not been replaced by alternative work.

If there are multiple attempts shown, then all attempts should be marked and the highest score on a single attempt should be awarded.

# • Follow through marks

Follow through marks which involve a single stage calculation can be awarded without working since you can check the answer yourself, but if ambiguous do not award.

Follow through marks which involve more than one stage of calculation can only be awarded on sight of the relevant working, even if it appears obvious that there is only one way you could get the answer given.

#### Ignoring subsequent work

It is appropriate to ignore subsequent work when the additional work does not change the answer in a way that is inappropriate for the question: eg. incorrect cancelling of a fraction that would otherwise be correct.

It is not appropriate to ignore subsequent work when the additional work essentially shows that the candidate did not understand the demand of the question.

#### • Linear equations

Full marks can be gained if the solution alone is given, or otherwise unambiguously indicated in working (without contradiction elsewhere). Where the correct solution only is shown substituted, but not identified as the solution, the accuracy mark is lost but any method marks can be awarded.

# Parts of questions

Unless allowed by the mark scheme, the marks allocated to one part of the question CANNOT be awarded in another

Question	Working	Answer	Mark	Notes
<b>1</b> (a)	$360 \div 10 = 36$	144°	2	M1 Any fully correct method to achieve
	180 - 36 = 144			interior angle of decagon.
	OR			A1
	$(2 \times 10 - 4) \times 90 \div 10$			
(b)	Let <i>X</i> be the foot of the perpendicular	from $B$ to $AD$	3	M1 allow "126" and "18" following from
	$(AX = )6\cos(180 - "144") (= 4.85)$			their144
	OR $(AX =) 6 \sin ("144" - 90)$			
	OR $(AC \text{ or } BD =) \frac{6 \sin 144}{\sin 18} (= 11.4)$			
	OR (AC or BD=) $\sqrt{6^2 + 6^2 - 2 \times 6 \times 6}$	<cos144< td=""><td></td><td></td></cos144<>		
	$OR \frac{AD}{\sin 126} = \frac{6}{\sin 18}$			
	$AD = 2 \times "4.85" + 6$			M1 dep allow "126" and "18" following
	"11.4" $\sin(180 - 144")$			from their"144"
	OR $AD = \frac{"11.4"\sin(180 - "144")}{\sin(126)}$			
	OR $AD = \sqrt{11.4^{12} + 6^2 - 2 \times 11.4^{12}}$	$6 \times \cos 126$		
	$OR AD = \frac{6\sin 126}{\sin 18}$			
	sin18			
		15.7 cm		A1 awrt 15.7 scores M1M1A1
				Total 5 marks

Question	Working	Answer	Mark	Notes
<b>2</b> (a)		Correct diagram	2	B1 for x and y correctly placed
				B1 ft their " $x$ " and " $y$ " for $12 - "x" - z$ ,
				6 - x" - y", $11 - z$ - y" all correct do
				not need to be simplified
				NB Mark diagram only
(b)	"x" + "y" + z = 11	27	3	M1 ft diagram may be implied by their
				working or answer
	Adding all the regions gives			M1 ft diagram as long as all sections
	38 - x - y - z = 38 - (x + y + z)			contain an entry
	OR $65 - 11 - 2 \times 9$			DO NOT ALLOW $65+x+y+z$ oe. For this
				mark or the A mark.
				A1 ft diagram as long as all sections
				contain an entry and final answer purely
				numerical.
				Total 5 marks

Question	Working	Answer	Mark	Notes
<b>3</b> (a)	$\tan x = \frac{110}{600}$	10.4°	2	M1 Fully correct expression involving angle APT
(b)	$(AQ^2 =)600^2 + 900^2 - 2 \times 600 \times 900 \cos 65^\circ$ $(AQ^2 =) 713572$	845 m	3	A1 awrt M1 Correct substitution into a correct cosine rule formula. M1 dep correct order of evaluation must see correct final answer or 713 000 to 714 000 inclusive or 456 000 to 457 000 inclusive in working to secure this mark.
(c)	$600^{2} + "845"^{2} - 2 \times 600$ $\times "845" \cos PAQ$ $(\cos PAQ = 0.260)(PAQ = 75)$ $OR                                    $	285°	3	A1 awrt M1 Correct trig equation leading to PAQ or APQ  M1 dep finding a bearing
	Bearing = 300 /3 01 100 / 03 / 40			A1 awrt
				Total 8 marks

Question	Working	Answer	Mark	Notes
<b>4</b> (a)	$(y = kT^2) 1600 = k \times 2.5^2$	5184	3	M1
	OR $\frac{y}{1600} = \left(\frac{4.5}{2.5}\right)^2$			
	$k = \frac{1600}{2.5^2} (= 256)$			M1 dep
	$R = \frac{1}{2.5^2} (= 256)$			A1 Accept 5180 with working seen
	OR $(y=)$ " $\frac{1600}{2.5^2}$ " $\times 4.5^2$			
(b)	$(y = Kr^3)$ so $K = \frac{12.5}{0.5^3}$ (=100) or $12.5 = K \times 0.5^3$	400	4	M1 can be implied by a fully correct calculation for r
	$("100" r^3 = y =)"256" \times 5000^2$			M1 indep oe.
				M1 oe correct calculation for <i>r</i>
	$r = \sqrt[3]{\frac{"256" \times 5000^2}{"100"}}$			dep on both previous M marks.
	γ "100"			NB Method for $r^3$ without clear
				evidence of cube root taken not
				sufficient. We must see a $\sqrt[3]{}$ symbol or
				their $r$ must be the cube root ir their $r^3$ .
				A1
				Total 7 marks

Question	Working	Answer	Mark	Notes
<b>5</b> (a)		Q correct	1	B1 <i>Q</i> drawn correctly Penalise lack of label once only on this question.
(b)		R correct	3	M1 for $y = x$ drawn and one correct pair of correct coordinates OR 2 correct coordinates A1 at least 3 pairs of correct coordinates A1 all correct including label.
(c)	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	S correct	3	M1 ft Their R Multiply all coordinates as vectors or in a matrix, must be correct order of multiplication. A1 ft R All points calculated correctly (possibly in matrix or vector form) OR 3 points correctly plotted A1 ft R All correct including label. Correct answer with no incorrect working scores full marks. ft their R. NB A correctly ft rotation of 90° anticlockwise of their R score full marks.
(d)	$ \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix} \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} $	$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$	2	M1 Correct Matrix $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$ multiplied by $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ (Condone incorrect order)  OR 3 elements of final matrix given correctly.  Done not award for $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ A1 cao isw incorrect subsequent working, checking the matrix transforms Q to S  Total 9 marks

<b>Working</b>			Notes
$\frac{800\ 000}{200} \times \frac{62}{100}$	2480	2	M1 Full method for 2480
Income yr 1 "2480" × 270 (= £669 600)	\$ 399704	6	M1
Income yr 2 (i) $(4000 - "2480") \times \frac{70}{100} \times 220 (= 234\ 080)$ Income yr 2 (ii) $\left(4000 - "2480" - (4000 - "2480") \times \frac{70}{100}\right) \times 150 \ (=68\ 400)$			M1 indep Both parts of yr 2
Total income in £ ("669 600"+"234080"+"68400"=972080)			
Total income in \$ "972 080" × 1.30 = 1 263704			M1 indep (Any attempt to convert an amount of £ to \$)
Borrowings + interest = 800000×1.08 = \$864000			M1 indep
Profit = \$"1263704" - "\$864000"			M1 dep all previous M marks A1 cao NB Ignore labelling or (a) and (b) in this question. Award marks wherever gained.  Total 8 marks
	Income yr 2 (i) $(4000 - "2480") \times \frac{70}{100} \times 220 (= 234\ 080)$ Income yr 2 (ii) $(4000 - "2480" - (4000 - "2480") \times \frac{70}{100}) \times 150 \ (=68\ 400)$ Total income in £ $("669\ 600" + "234080" + "68400" = 972080)$ Total income in \$ $"972\ 080" \times 1.30 = 1\ 263704$ Borrowings + interest = $800\ 000 \times 1.08 = \$864\ 000$	Income yr 2 (i) $(4000 - "2480") \times \frac{70}{100} \times 220 (= 234\ 080)$ Income yr 2 (ii) $(4000 - "2480" - (4000 - "2480") \times \frac{70}{100}) \times 150 \ (=68\ 400)$ Total income in £ $("669\ 600" + "234080" + "68400" = 972080)$ Total income in \$ $"972\ 080" \times 1.30 = 1\ 263704$ Borrowings + interest = $800\ 000 \times 1.08 = \$864\ 000$	Income yr 2 (i) $(4000 - "2480") \times \frac{70}{100} \times 220 (= 234\ 080)$ Income yr 2 (ii) $(4000 - "2480" - (4000 - "2480") \times \frac{70}{100}) \times 150 \ (=68\ 400)$ Total income in £ $("669\ 600" + "234080" + "68400" = 972080)$ Total income in \$ $"972\ 080" \times 1.30 = 1\ 263704$ Borrowings + interest = $800\ 000 \times 1.08 = \$864\ 000$

Question	Working	Answer	Mark	Notes
<b>7</b> (a)	$A = 2\pi rh + \pi r^2 + \frac{1}{2} \times 4\pi r^2$ $OR A = \pi r (2h+r) + \frac{1}{2} \times 4\pi r^2$	Shown	1	B1 Allow $2\pi r^2$ for $\frac{1}{2} \times 4\pi r^2$ but must see hemisphere and cylinder separately. Do not accept $4\pi r^2 - \pi r^2$
(b)	$(V =) \pi r^2 h - \frac{2}{3} \pi r^3$ $(h =) \frac{1300\pi - 3\pi r^2}{2\pi r}$ $V = \pi r^2 \left(\frac{1300\pi - 3\pi r^2}{2\pi r}\right) - \frac{2}{3} \pi r^3$ $V = 650\pi r - \frac{13}{6} \pi r^2$	shown	4	M1 Make h the subject allow 1 sign or arithmetic error.  NB We must see a clear expression for $h$ (may be inferred from substituted expression in $V$ ) after cancelling  M1 dep (on B1 and M1) for substitute for $h$ in $V$ A1 Answer Given  Must include at least one correct intermediate step following the $2^{\text{nd}}$ M mark  eg. $V = \frac{\pi r^2 1300\pi}{2\pi r} - \frac{3}{2}\pi r^3 - \frac{2}{3}\pi r^3$
(c)	$\left(\frac{dV}{dr} = \right) 650\pi - \frac{13}{2}\pi r^2 = 0$ $V = 650\pi \times 10 - \frac{13}{6}\pi \times 10^3$	10 13 000π	2	M1 for attempting to differentiate and setting = 0 must see at least one term correct. =0 can be inferred from their working.  A1 cao do not allow ±10  M1 for substituting for their <i>r</i> into <i>V</i> or finding
	$r = 650 n \times 10 = \frac{1}{6} n \times 10$	3		h from their r and using this to find V  A1 oe (Must be exact) Accept $4333\frac{1}{3}\pi$ or  4333. $3\pi$ Total 9 marks

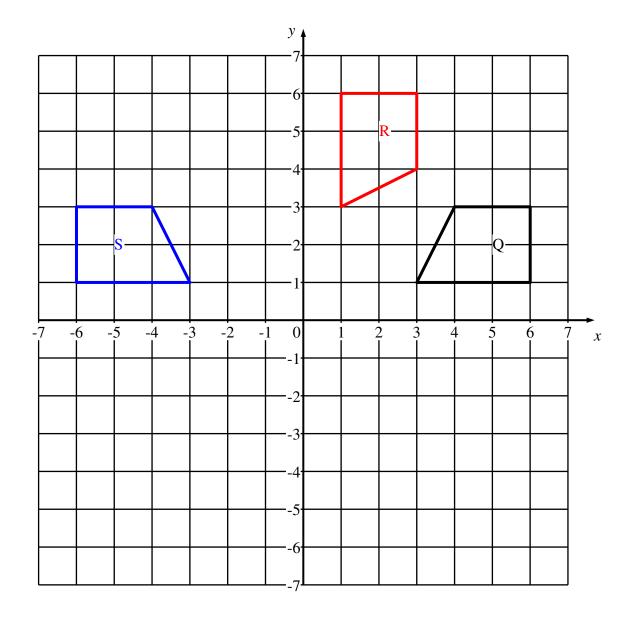
Question	Working	Answer	Mark	Notes
<b>8</b> (a)		-1	1	B1
(b)	$gf(x) = (2x-5)^{2}$ $4x^{2} - 20x + 25 = 30$ or $4x^{2} - 20x - 11 = 0$ OR $f(x) = (\pm)6$	$x = \frac{11}{2}$ only	3	M1
	$(2x-11)(2x+1) = 0 \text{ OR } 2x-5 = (\pm)6$ $OR(x=) \frac{-(-20) \pm \sqrt{(-20)^2 - 4 \times 4 \times (-11)}}{2 \times 4}$			A1 Award A0 if $x = -\frac{1}{2}$ given as a solution and not rejected.
(c)(i)	$(f^{-1}(x) =) \frac{x+5}{2}$ $OR                                    $	$x = \frac{5 + 10\lambda}{4\lambda - 1}$	5	B1 Inverse function seen or fully correct statement from which <i>x</i> could be found without using inverse seen.  M1 Fully correct equation. FT their inverse.  M1 dep (B and M marks) Terms in <i>x</i> isolated on one side Allow a maximum of 1 sign error A1 oe
(ii)		$\frac{1}{4}$		B1 ft Rational expression with λ in denominator from part (i)
	I	· · · · · · · · · · · · · · · · · · ·	1	Total 9 marks

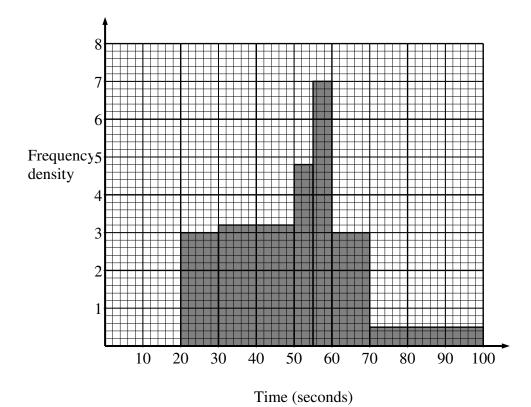
Question	Working	Answer	Mark	Notes
<b>9</b> (a)(i)		<b>−6a</b>	2	B1 oe
(ii)		6 <b>b"</b> –6 <b>a"</b>		B1 oe ft (i)
(b)	$\overrightarrow{XC} = 6\mathbf{b} - 15\mathbf{a} \ \mathbf{OR} \ \overrightarrow{CX} = 15 \ \mathbf{a} - 6 \ \mathbf{b}$	Shown	2	M1 ft (a)
	$\overrightarrow{OG} = \overrightarrow{OX} + \overrightarrow{XG} = \overrightarrow{OX} + k\overrightarrow{XC} =$			A1 for a complete method (Answer Given)
	$\overrightarrow{OX} + k(\overrightarrow{OC} - \overrightarrow{OX}) = 9\mathbf{a} + k(6\mathbf{b} - 6\mathbf{a} - 9\mathbf{a})$			
	$\overrightarrow{OG} = 6k\mathbf{b} + (9 - 15k)\mathbf{a}$			
(c)	$9-15k=0\;,$	$\frac{18}{5}$ <b>b</b>	2	M1
	$\overrightarrow{OG} = 6 \times \frac{3}{5} \mathbf{b}$			A1 oe
(d)	$\overrightarrow{OH} = \overrightarrow{OA} + \overrightarrow{AH} = \overrightarrow{OA} + p\overrightarrow{AC} =$	m = 9 $n = 5$	4	M1 Find expression for $\overrightarrow{OH}$ in terms of $\mathbf{a}$ ,
	$\overrightarrow{OA} + p(\overrightarrow{OC} - \overrightarrow{OA}) =$	n=3		<b>b</b> and "p" Also award if one of the following seen:
	$12\mathbf{a} + p(6\mathbf{b} - 6\mathbf{a} - 12\mathbf{a}) = 6p\mathbf{b} + (12 - 12\mathbf{a})$			OG:OB=3:2 or OG:OB=3:5
	18p) <b>a</b>			or GB:OB = 2:5 Accept any valid ratio.
	$12 - 18p = 0  p = \frac{2}{3}$			M1 dep. Valid method to find "p"
	OC CH HD 18 4 18 6 4			M1 dep Correct ratio given in any form
	$OG:GH:HB = \frac{18}{5}:4 - \frac{18}{5}:6 - 4$			A1 accept 9:1:5
	OR $\frac{2}{5}$ $OG = \frac{18}{5}$ $GH$ and $2 OG = \frac{18}{5}$ $GH$			
				Total 10 marks

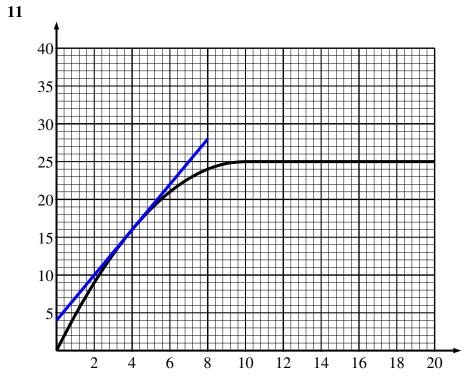
Question	Working	Answer	Mark	Notes
<b>10</b> (a)	Use of at least 3 correct midpoints		4	M1
	$\Sigma fT = 25 \times 70 + 35 \times 130 + 45 \times 210 +$	50.6 seconds		M1 indep values of <i>T</i> in the
	$55 \times 160 + 65 \times 130 + 75 \times 100 $ (=40500)			interval, including ends and used
				consistently (EG all minimum
				values) allow a maximum of one
				incorrect/missing term.
	"40500" ÷ 800			M1 dep 2nd M marks
				A1 awrt
				Allow 51 if a fully correct
				expression seen in working.
(b)	FDs 3, 3.2, 4.8, 7, 3, 0.5	Fully correct	3	M1 for any correct calculation of
		histogram		a FD
				A1 All correct FD or 3 correct
				bars
				A1 all correct allow ½ small
				square tolerance on all bars. Bars
				must touch.
(c)	$30 + \frac{5}{100} \times 64$	46	2	M1 n must be greater than their
	$\frac{30+\overline{20}}{20}$	198		numerator.
	n			ft 3.2 as value of FD of their 2 <sup>nd</sup>
	$(35-30)\times 3.2+64$			bar.
	or $\frac{n}{n}$			A1 oe $\frac{23}{99}$ , 0.232 or better.
				Total 9 marks
				10iai 9 marks

Question	Working	Answer	Mark	Notes
<b>11</b> (a)	$25 \times \frac{60 \times 60}{1000}$	90	2	M1 Fully correct expression A1 cao
(b)	Draw tangent at $t = 4$ Gradient = $\frac{28 - 4}{8}$	3 m/s <sup>2</sup>	3	M1 a clear intention to draw a tangent at the point $t = 4$ M1 dep ft Their drawn tangent, if no tangent drawn do not award mark. A1 2.5 - 3.5 NB. Correct answer within allowed range with no incorrect working seen scores M1M1A1
(c)	SC: Straight line drawn from (2,10) to (4,10) and straight line drawn from (4,10) to (18,10) award B0B1	Correct graph	2	B1 Straight line joining (2,10) to (6, 10) Ignore anything to the left of t=2. Allow 1 small square tolerance.  B1 Straight line joining (6,10) to (20, 20) Allow 1 small square tolerance.
(d)	Area under van graph = $10 \times 4 + \frac{10 + 20}{2} \times 14 = 40 + 210$ $416\frac{2}{3}$ -"250"	$166\frac{2}{3}$	3	M1 ft, correct expression to find area under their "curve" strictly to the right of $t$ =2 allow a maximum of 1 error.  NB graph may stop before $t$ =20  M1 (dep) Allow 416.6 to 416.7 for $416\frac{2}{3}$ A1 oe $\frac{500}{3}$ Allow 166.6 to 166.7
				Total 10 marks

Question	Working	Answer	Mark	Notes
<b>12</b> (a)		-2, -1.5, 5.7	3	B1, B1, B1 cao
(b)		-2.5	3	Treat as B3 ft (-1EEOO) -1 mark for straight line segments (penalise ONCE only on segments between x=1 and x=2) each point missed each missed segment each point not plotted each point incorrectly plotted tramlines (penalise ONCE only) very poor curve (penalise ONCE only) Allow ½ a small square tolerance on all points.  B1 Accept -2.42.6 or ft as long as the value is from a turning
				point on the curve.
(d)	$x^{3} - 2x^{2} - 6x + 5 = 0 \implies$ $x^{2} - 2x - 6 + \frac{5}{x} = 0$ $\Rightarrow x^{2} - 8 + \frac{5}{x} = 2x - 2$	0.7, 3.3	4	M1 oe dividing by x  NB Allow a total of one sign error across both of these two marks  M1 dep Isolating $x^2 - 8 + \frac{5}{x}$
	Draw $y = 2x - 2$ and find at least one intersection			M1 Draw their line as long as is in the form $y = \pm 2x + c$ (allow $c=0$ )  A1 Allow 0.6-0.8 and 3.2-3.4  NB must have evidence of correct working, a minimum of a non-horizontal straight line drawn.  Total 11 marks







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